FORMULA FOR TRUE ANIMAL PREVALENCE:

$$\pi^{\mathrm{A}} = \frac{p^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1}{\mathrm{Se}^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1},$$

FORMULA FOR TRUE HERD PREVALENCE:

$$\pi^{\mathrm{H}} = \sum_{n_{i}=0}^{\infty} P(n_{i}) \left(1 - \prod_{k=0}^{n_{i}-1} \left[1 - \frac{p^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1}{\mathrm{Se}^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1} + \frac{k(p^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1)\rho}{\{1 + (k-1)\rho\}(\mathrm{Se}^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1)} \right] \right)$$
$$= \sum_{n_{i}=0}^{\infty} P(n_{i}) \left(1 - \prod_{k=0}^{n_{i}-1} \left[1 + \frac{(p^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1)(\rho - 1)}{(\mathrm{Se}^{\mathrm{A}} + \mathrm{Sp}^{\mathrm{A}} - 1)\{1 + (k-1)\rho\}} \right] \right).$$

EXPLANATION OF THE NOTATION USED IN THE ABOVE FORMULA:

- n_i = Number of Animals in herd i
- z_i = Number of positively tested Animals in herd i
- π^{A} = True Animal Prevalence
- π^{H} = True herd Prevalence
- Se = Sensitivity of a single test
- Sp = Specificity of a single test
- P^A = Apparent Animal Prevalence
- P^H = Apparent herd Prevalence
- Se^H = Herd Sensitivity
- Sp^H = Herd Specificity
- ρ = Herd Correlation
- k = number of Herds